In the Claims:

The claims are as follows:

- 1. (Previously presented) A method of determining, in a computer environment, the equivalence, if any, of two algebraic expressions for use in compiler optimisation of source code and like computing tasks, said method comprising the steps of:
- (a) recasting said expressions into a form of one or more token pairs arranged sequentially in a string, each said token pair comprising an operator followed by an operand;
 - (b) reducing said strings in accordance with a set of predetermined simplifying rules;
- (c) comparing the reduced strings by matching, to detect equivalence of the two algebraic expressions; and
- (c1) compiling said source code into object code, wherein said source code comprises said two algebraic expressions, and wherein said compiling comprises said recasting, said reducing, and said comparing.
- 2. (Previously presented) The method of claim 1, whereby the recasting step (a) is preceded by a preconditioning step comprising, in relation to said algebraic expressions, the following substeps according to whether a sub step applies:
 - (da) deleting a space in the expression;
 - (db) removing a bracket in the expression by expanding a bracketed sub-expression;
 - (dc) inserting a unitary operator at the start of the expression;
 - (dd) recasting a power factor, being a variable being raised to a power in the

expression, in an alternate form as one of:

- (dda) the power factor being expressed as the variable multiplied by itself as many times as the power, if the power is a positive integer;
- (ddb) the power factor being expressed as a reciprocal of the variable multiplied by itself as many times as an absolute value of the power, if the power is a negative integer;
- (ddc) the power factor being replaced by an appropriate function which can compute the power factor, if the power is not an integer;
 - (de) recasting a constant in the expression in exponential format;
- (df) substituting a "+" operator in the expression by "+1*", a "1" being in exponential format;
- (dg) substituting a "-" operator in the expression by "-1*", a "1" being in exponential format; and
- (dh) recasting a "division by a constant" in the expression as multiplication by a reciprocal of the constant.
- 3. (Previously presented) The method of claim 1, whereby the simplifying rules in step (b) comprise:
 - (ba) arranging token pairs into subgroups;
 - (bb) arranging operand tokens in an arranged subgroup in order;
- (bc) reducing the ordered operands by consolidating one or more constants and eliminating variables of opposite effect to form reduced subgroups; and
 - (bd) consolidating one or more multiple instances of similar subgroups, to produce a

reduced string.

4. (Previously presented) The method of claim 1, whereby an algebraic expression whose equivalence is to be determined contains an aliased variable, said method further comprising the steps of:

arranging an ordered list of aliases of the variable, and substituting a first alias in the ordered list for all instances of the aliased variable in the expression.

5. (Previously presented) The method of claim 1, whereby an algebraic expression whose equivalence is to be determined contains a function, said method further comprising the steps of:

reducing function arguments using the set of predetermined simplifying rules; and replacing the function by a tagged string, said string designating a function name, parameter types, and arguments, whereby the tag distinguishes the function name from a variable.

- 6. (Previously presented) An apparatus adapted to determine, in a computer environment, the equivalence, if any, of two algebraic expressions for use in compiler optimisation of source code and like computing tasks, said apparatus comprising:
- (a) recasting means for recasting said expressions into a form of one or more token pairs arranged sequentially in a string, each said token pair comprising an operator followed by an operand;
- (b) reduction means for reducing said strings in accordance with a set of predetermined simplifying rules;

- (c) comparison means for comparing the reduced strings by matching, to detect equivalence of the two algebraic expressions; and
- (c1) means for compiling said source code into object code, wherein said source code comprises said two algebraic expressions, and wherein said means for compiling comprises said means for recasting, said means for reducing, and said means for comparing.
- 7. (Previously presented) A computer program product including a computer readable medium having recorded thereon a computer program for determining, in a computer environment, the equivalence, if any, of two algebraic expressions for use in compiler optimisation of source code and like computing tasks, said computer program comprising:
- (a) recasting process steps for recasting said expressions into a form of one or more token pairs arranged sequentially in a string, each said token pair comprising an operator followed by an operand;
- (b) reduction process steps for reducing said strings in accordance with a set of predetermined simplifying rules;
- (c) comparison process steps for comparing the reduced strings by matching, to detect equivalence of the two algebraic expressions; and
- (c1) compiling process steps for compiling said source code into object code, wherein said source code comprises said two algebraic expressions, and wherein said compiling comprises said recasting, said reducing, and said comparing.
- 8. (Previously presented) The method of claim 1, wherein said reduction process steps comprise:

processing token pairs into an ordered arrangement;

determining whether a redundant equivalent subexpression exists within said ordered arrangement; and

if said determining determines that said redundant equivalent subexpression exists within said ordered arrangement, then eliminating said redundant equivalent subexpression from said ordered arrangement.

9. (Canceled)

- 10. (Previously presented) The apparatus of claim 6, whereby the simplifying rules in step (b) comprise:
 - (ba) arranging token pairs into subgroups;
 - (bb) arranging operand tokens in an arranged subgroup in order;
- (bc) reducing the ordered operands by consolidating one or more constants and eliminating variables of opposite effect to form reduced subgroups; and
- (bd) consolidating one or more multiple instances of similar subgroups, to produce a reduced string.
- 11. (Previously presented) The apparatus of claim 6, whereby an algebraic expression whose equivalence is to be determined contains an aliased variable, said apparatus further comprising means for arranging an ordered list of aliases of the variable, and substituting a first alias in the ordered list for all instances of the aliased variable in the expression.

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12. (Previously presented) The apparatus of claim 6, whereby an algebraic expression whose equivalence is to be determined contains a function, said apparatus further comprising:

means for reducing function arguments using the set of predetermined simplifying rules; and

means for replacing the function by a tagged string, said string designating a function name, parameter types, and arguments, whereby the tag distinguishes the function name from a variable.

13. (Previously presented) The apparatus of claim 6, wherein said reduction means comprises: means for processing token pairs into an ordered arrangement;

means for determining whether a redundant equivalent subexpression exists within said ordered arrangement; and

means for eliminating said redundant equivalent subexpression from said ordered arrangement.

14. (Canceled)

- 15. (Previously presented) The computer program product of claim 7, whereby the simplifying rules in step (b) comprise:
 - (ba) arranging token pairs into subgroups;
 - (bb) arranging operand tokens in an arranged subgroup in order;
 - (bc) reducing the ordered operands by consolidating one or more constants and

eliminating variables of opposite effect to form reduced subgroups; and

(bd) consolidating one or more multiple instances of similar subgroups, to produce a reduced string.

16. (Previously presented) The computer program product of claim 7, whereby an algebraic expression whose equivalence is to be determined contains an aliased variable, said computer program further comprising the steps of:

arranging steps for arranging an ordered list of aliases of the variable, and substituting steps for substituting a first alias in the ordered list for all instances of the aliased variable in the expression.

17. (Previously presented) The computer program product of claim 7, whereby an algebraic expression whose equivalence is to be determined contains a function, said computer program further comprising the steps of:

reducing steps for reducing function arguments using the set of predetermined simplifying rules; and

replacing steps for replacing the function by a tagged string, said string designating a function name, parameter types, and arguments, whereby the tag distinguishes the function name from a variable.

18. (Previously presented) The computer program product of claim 7, wherein said reduction process steps comprise:

processing steps for processing token pairs into an ordered arrangement;

determining steps for determining whether a redundant equivalent subexpression exists within said ordered arrangement; and

eliminating steps for eliminating said redundant equivalent subexpression from said ordered arrangement.

19. (Canceled)